



REVIEW PAPER

Wells turbine for wave energy conversion: a review

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SUMMARY

In the past 20 years, the use of wave energy systems has significantly increased, generally depending on the oscillating water column concept. Wells turbine is one of the most efficient oscillating water column technologies. This article provides an updated and a comprehensive account of the state-of-the-art research on Wells turbine. Hence, it draws a roadmap for the contemporary challenges, which may hinder future reliance on such systems in the renewable energy sector. In particular, the article is concerned with the research directions and methodologies, which aim at enhancing the performance and efficiency of Wells turbine. The article also provides a thorough discussion of the use of CFD for performance modeling and design optimization of Wells turbine. It is found that a numerical model using the CFD code can be employed successfully to calculate the performance characteristics of W-T as well as other experimental and analytical methods. The increase of research papers about CFD, especially in the last 5 years, indicates that there is a trend that considerably depends on the CFD method. Copyright © 2016 John Wiley & Sons, Ltd.

KEY WORDS

Wells turbine; CFD; wave energy; oscillating water column

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1. INTRODUCTION

Generating renewable energy has been increasing considerably in the past decade, achieving almost 22% of the global energy production in 2013, compared with 14% in 2005 [1]. The ocean is a potential goldmine for renewable energy generation for several reasons, most important of which is that, unlike wind and solar power, power from ocean waves continues to be produced around the clock [2]. In addition, wave energy varies with the square of wave height, whereas wind energy varies with the cube of air speed. This results in a much higher average power production from waves per unit of time [3]. Moreover, marine waves travel great distances without significant energy losses, so they act as a renewable and an efficient energy transport mechanism across thousands of kilometers. Such renewable energy can be produced through different devices, which produce sufficient work to drive electrical generators that convert such work into electricity. Wave energy extractors can be classified according to the water depth at which they operate. This classification is presented

in Figure 1. Another classification based mostly on working principle is presented in Table I.

Most of fixed-structure oscillating water column (OWC) systems are located on the shoreline or near the shore. Shoreline devices are characterized by relatively easier maintenance and installation, and they do not require deep water moorings and long underwater electrical cables. The floating OWC devices are slack-moored to the sea bed and so are largely free to oscillate, enhancing the wave energy absorption if the device is properly designed for that purpose [4].

Offshore devices are basically oscillating bodies, either floating or fully submerged. They take advantage of the most powerful wave systems available in deep water. Offshore wave energy converters are in general more complex compared with fixed-structure OWC. This, together with additional problems related to mooring and access for maintenance and the need of long underwater electrical cables, has hindered the converters' development, and only recently have some systems reached, or come close to, the full-scale demonstration stage [5].

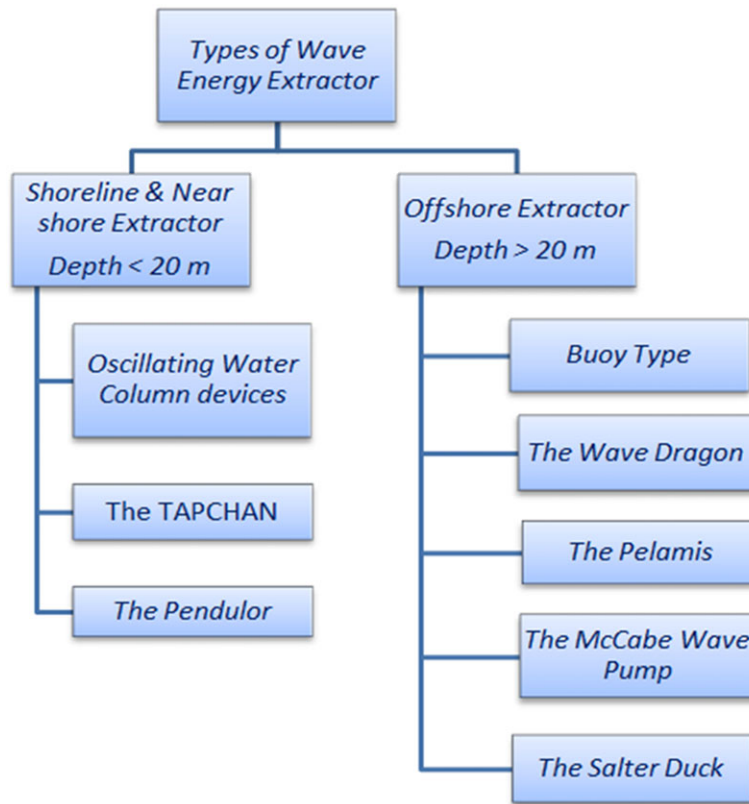


Figure 1. Types of wave energy extractors with respect to water depth.

Table I. Types of wave energy extractors based on working principle [6].

System	Energy extractor	Structure types	Example	Remark
Oscillating water column	Air turbine	Fixed structure	Pico LIMPET Sakata Mutriku	Isolated Breakwater
		Floating	Mighty Whale Sperboy Oceanlinx	—
Oscillating bodies	Hydraulic motor, hydraulic turbine and linear electrical generator	Floating	AquaBuoy IPS Buoy FO3 Wavebob PowerBuoy	Essentially translation
			Pelamis PS Frog SEAREV	Essentially rotation
		Submerged	AWS WaveRoller Oyster	Essentially translation Rotation with bottom hinged
			TAPCHAN SSG	Shoreline Breakwater
Overtopping	Low head hydraulic turbine	Fixed structure	TAPCHAN SSG	Shoreline Breakwater
		Floating	Wave Dragon	—

Overtopping systems are a different way of converting wave energy to capture the water that is close to the wave crest and introduce it, by overspilling, into a reservoir

where it is stored at a level higher than the average free-surface level of the surrounding sea [6,7]. The potential energy of the stored water is converted into useful energy

through more or less conventional low-head hydraulic turbines. The hydrodynamics of overtopping devices is strongly nonlinear and, unlike the cases of oscillating body and OWC wave energy converters, cannot be interpreted by linear water wave theory.

OWC energy converters operate much like a wind turbine via the principle of wave induced air pressurization [8–10]. A containment housing (air chamber) is placed above the water, allowing the passage of waves to change the water level. The frequently rising and falling water level increases and decreases the air pressure, respectively, within the housing. With regard to this notion, a turbine could be placed on top of the housing through which air may pass. Air would flow into the housing during a wave trough and out of the housing during a wave crest. Such operation principle is illustrated in Figure 2(a). Because of this bidirectional air flow, the turbine must be designed to rotate only in one direction, regardless of the air flow direction [6,7,11].

Finding an efficient and an economical means of converting oscillating flow energy to unidirectional rotary motion for driving electrical generators is the major challenge facing OWC systems. A novel solution for such a challenge is the W-T [12–16], a version of the axial-flow turbine. W-T is named after Professor Alan Wells of the Queen's University of Belfast in the 1980s. It is unique as it contains a rotor with untwisted airfoil blades of symmetrical cross section, usually belonging to the symmetrical NACA four-digit series [17–20], see Figure 2(b). A

typical W-T consists of a rotor with about eight airfoil sectioned blades, installed on the hub with their chord lines lying in the plane of rotation. Once the blades have attained design speed, the turbine produces with a fair efficiency a time-averaged positive power output from the oscillating air flow [4,21].

The W-T is one of the simplest and probably the most economical turbines for wave energy conversion. It does not require rectifying air valves and can extract power at a low airflow rate, when other turbines would be inefficient. Therefore, it has been extensively researched and developed in many countries. Most self-rectifying air turbines for wave energy conversion proposed and tested so far are axial-flow machines of two basic types: the W-T and the impulse turbine. The impulse turbine was patented by I. A. Babintsev in 1975 [22]. Its rotor is basically identical to the rotor of a conventional single-stage steam turbine of axial-flow impulse type. Because the turbine is required to be self-rectifying, there are two rows of guide vanes, placed symmetrically on both sides of the rotor, instead of a single row. These two rows of guide vanes are the reflection of each other, with respect to a plane through the rotor disk [23–25]. Therefore, it is more complex and more costly than W-T. The efficiency of W-T is higher than that of the impulse turbine when the flow coefficient is less than the stall point. But after the stall point of W-T, the efficiency of impulse turbine is considerably higher than that of W-T. However, the peak efficiencies are almost the same [26].

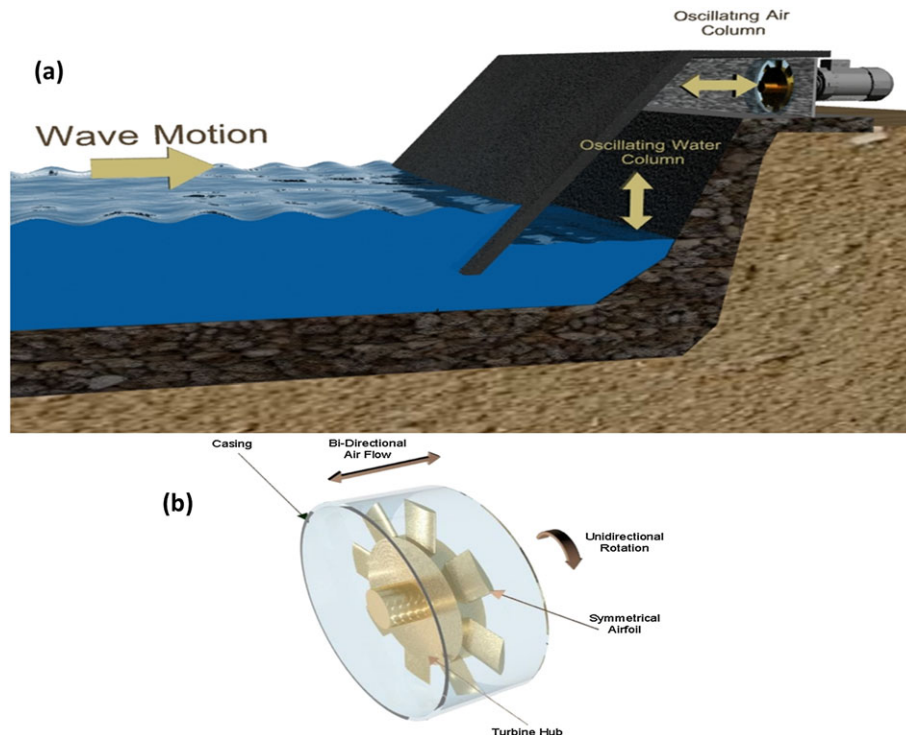


Figure 2. Oscillating water column energy converters: (a) an illustration of the principle of operation of oscillating water column system, where the wave motion is used to drive a turbine through the oscillation of air column [108] and (b) typical structure of W-T rotor [108].

It is worth mentioning that the W-T (with or without guide vanes) and the contra-rotating W-T are approximately a linear turbine (i.e., the pressure drop is approximately proportional to the flow rate at constant rotational speed). Other turbines behave quite differently (like impulse turbines) [18]. The principle of W-T is explained in details later in this section.

The main objective of this review is to provide an updated account, as comprehensive as possible, of the state-of-the-art research on W-T. This article also intends to provide a self-contained reference for the broadest readership possible within the renewable energy community. The authors have studied all the available research publications related to W-T and conducted a thorough categorization exercise to establish a roadmap for the research directions in the topic. This roadmap is based on the W-T system components on the one hand, and on the research approach and methodology of each reference work on the other hand. Therefore, Section 1 is dedicated to explain the operation principle, cycle and energy analysis of W-T. A review of existing W-T projects is presented in Section 2. Sections 3 and 4 review and discuss the design parameters of W-T and the works performed to improve their performance through the optimization and modification of such parameters. Because a significant percentage of research utilized CFD to simulate W-T, Section 5 is dedicated to review and discuss these efforts. In Section 5, CFD research works are categorized according to model complexity and physical assumptions. Such categorization, accompanied by a critical discussion of modeling approaches, is intended to

highlight the state-of-the art knowledge for the multidimensional modeling of W-T. Section 6 provides a critical discussion and draws a research roadmap in conclusion of the article.

1.1. Operation principle of W-T

The characteristic feature of W-T is that oscillating air flow produces a single direction rotation of the rotor without the use of a rectifying valve. It is usually characterized by four-digit double zero NACA profiles [27–29], where the shape of the NACA four-digit profiles is determined by three parameters: the camber (first digit), the position of the camber (second digit), and the thickness in percent of the chord (last two digits). Hence, profiles without a camber are symmetrical (NACA 00XX). According to the classical airfoil theory, an airfoil set at α in a fluid flow generates L , normal to the free stream. The airfoil also experiences D , in the direction of the free stream, see Figure 3(a) and (b). For real fluids, Lift and Drag increase with the increase in α ; however, only up to a certain value of α beyond which the flow around the airfoil separates. The angle of incidence at which the flow separates from the surface of the airfoil is known as the stall angle [30], see Figure 3 (c). Further increase in α beyond the stall angle results in a decrease in lift and a significant increase in drag [16,21,28]. Because the flow between adjacent blades in cylindrical or liner series of blades (cascade) can be quite different to that over isolated airfoils, the cascade lift and drag are different to those of isolated airfoil because of

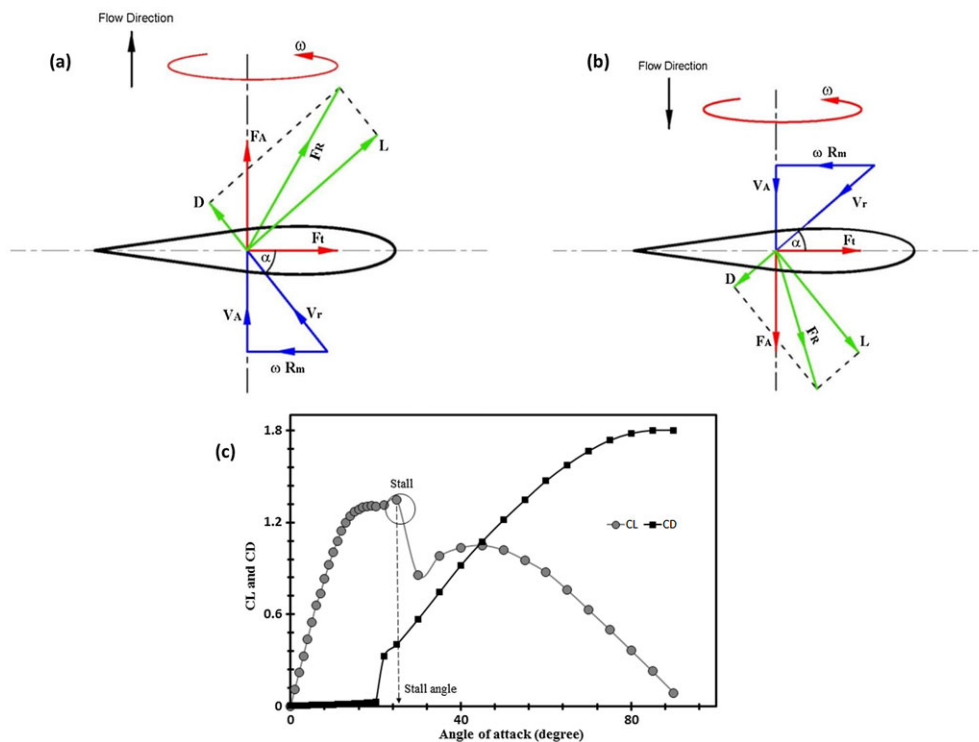


Figure 3. Aerodynamic forces: (a) compression stages, (b) suction stages, and (c) lift and drag coefficient variation with angle of attack [28].

the interference that each blade has on the flow field around its neighbors [31–33].

1.2. Operation cycle

The operation cycle of W-T is classified into two stages according to the action of the OWC. First, the compression stage, in which the water level rises inside the housing, see Figure 3(a). The resultant aerodynamic force F_R due to lift and drag forces is given by

$$F_R = \sqrt{L^2 + D^2} \quad (1)$$

This force can be decomposed in two components into axial and tangential directions in terms of lift and drag components as

$$F_A = L \cos \alpha + D \sin \alpha \quad (2)$$

and

$$F_t = L \sin \alpha - D \cos \alpha \quad (3)$$

where F_A and F_t are the axial and tangential forces, respectively.

Second, the suction stage, in which the water level drops, sucking air into the duct, and a similar velocity and force analysis can be described as shown in Figure 3(b). A comparison between Figure 3(a) and (b) shows that the tangential force maintains the same direction during the two stages, while the axial force reverses its direction. For a symmetrical airfoil section, the direction of tangential force F_t remains the same for both positive and negative values of α . Such airfoil blades are set around an axis of rotation. The rotor rotates in the direction of F_t or upward and downward strokes, regardless of the direction of airflow.

The vast majority of researchers assume that the force analysis resulting from the flow through the rotor can be reduced to a two-dimensional analysis. This assumption is based on the radial equilibrium theory [34,35] where the force resulting from the radial velocity component is assumed to be negligible everywhere in the flow field except within the blade rows [16]. Nevertheless, there have been some studies citing the relevance of the radial force components. In such studies, it was assumed that the force resulting from the radial velocity component was far from being negligible [36–38]. Also, Falcao *et al.* reported that a fully three-dimensional force analysis should be performed, or at least corrections to two-dimensional flow results should be introduced. In addition, it could be assumed that the radial force component is negligible, if the rotor blade work per unit mass is constant along the span or, equivalently, if the velocity circulation about the blades does not vary along the radial coordinate. However, such conditions, although very common, are not generally satisfied in self-rectifying turbines for OWC applications [18].

From the electrical power engineering point of view, the W-T system can be seen as an AC/AC converter, which converts a mechanical power signal with variable force and frequency into an electrical power signal with constant voltage

and frequency [39]. W-T converts the bidirectional airflow into mechanical energy in the form of unidirectional shaft power, which is in turn used to move the wound rotor induction machine. The wound rotor machine controlled by rotor resistance has several advantages, such as high line power factor, absence of line current harmonics, and smooth and wide range of speed control. As the external resistance is increased, the torque/slip curve becomes flatter, giving less speed, until the speed becomes zero at high resistance [40].

The squirrel cage induction generator is normally preferred because it is cheap, small, rugged, maintenance-free, and does not require separate excitation and synchronization to the grid. It works as a motor when running below synchronous speed, and as a generator above synchronous speed. However, the use of double-fed induction generator has a huge potential in the development of distributed renewable energy sources. The double-fed induction generator is essentially an asynchronous machine, but instead of the rotor windings being shorted (as in a squirrel-cage induction machine), it is arranged to allow an AC current to be injected into the rotor, via the power converter. By varying the phase and frequency of the rotor excitation, it is possible to optimize the energy conversion. The frequency converter only has to process the generator's slip power fraction, which is generally no more than 30% of the generator rated power. This reduced rating for the frequency converter implies an important cost saving, compared with a fully rated converter [40,41].

1.3. Evaluation of techno-economic aspects

The utilization of the sea wave was rarely considered on a practical scale prior to 1973. However, a great deal of research has been conducted since 1973, the year of the so-called oil crisis [42]. In recent years, interest has revived, particularly in Japan, Britain, and Scandinavia, so the research and small-scale development have progressed to the stage of commercial construction for power extraction. As with all renewable energy supplies, the scale of operation has to be determined, and present trends support moderate power generation levels at about 1 MW from modular devices about 50 m wide across the wave front. Such devices should be economic to replace diesel-generated electricity, especially on islands [7].

The predicted costs of wave power, in particular, have been falling against those of fossil fuels. The World Energy Council estimates that electricity from "arrays of mature devices located in promising wave energy sites" could cost from 5 to 10 cents/kWh. In fact, the Limpet, an on-shore OWC device, began commercially generating electricity in Scotland in late 2000. At the time, the expected cost of Limpet's electricity was 7 to 8 cents/kWh [43]. And according to the Electric Power Research Institute, the cost of ocean electricity production will drop significantly as the volume of production increases, as usually happens in the development and commercialization of any new technology. The electricity price produced from wave energy is still high but is forecasted to decrease

with the development of the technology. This can be speeded up with initial financial and market support as it has been performed in the past for preceding technologies such as wind, nuclear energy, and oil.

Energy production costs are a major drive for the development of wave power – the lower they are, the faster the market grows. There are several levers to bring down costs of energy production systematically [44–47], including, in order:

1. Reliability of the equipment. The degree of reliability of a wave power concept largely drives project risk, and thus, the rate at which an investor expects a new investment to earn. Therefore, reliability is an important key for the customer.
2. Efficiency of the machine. Costs per kilowatt-hour are, in simple terms, discounted cash-outflows for capital investments, operations, and maintenance, divided by discounted number of kilowatt-hours produced. Hence, an increase of energy output works on the total investment – not only the turbine – and can bring costs down considerably.
3. Reduction of capital investment costs. The largest cost item on an OWC plant is the collector. Bringing this cost down has a significant influence on energy production costs. Apart from creative engineering, the best idea is to avoid spending large sums on the collector by sharing it with other applications. This is how the idea of the active breakwater application was born.

For coastal protection, large concrete structures are built in order to protect harbors from waves. If these structures are modified so that OWCs can be included in the front wall, costs can be shared and, according to laboratory measurements, loads on the walls can be significantly reduced. For a caisson type breakwater, an empty concrete structure

with a rectangular structure of concrete enforcement walls is cast. In this state, the structures are floating and can be towed into position by a ship. The empty chambers are then filled with stones or sand so that the structure can sink and sit rigidly on the seabed. If the front chambers of the wall are only partly filled, and openings under water are included, an OWC chamber can be formed [48,49]. The W-T is placed into the airflow. In this configuration, the breakwater is converted into an active breakwater, which not only protects the coast but also produces energy. Harbors usually require a high level of electrical energy and therefore offer good opportunities for grid connection. In effect, a fully integrated engineering development approach would appropriately design a shoreline OWC in order to find the best compromise between cost and performance. Following this path would lead to differences between a W-T configuration, notably in terms of the OWC design and choice of location [50]. However, compared with W-T, other types of wave energy converters are more expensive and have more complex designs.

2. EXISTING W-T STATIONS

Since the 1970s, there have been a number of wave energy projects based on W-T. Table II provides a summary of all reported W-T projects. The LIMPET [51–56] and Pico projects [57–62] are shoreline mounted systems. The OSPREY [63] is an example of near shore W-T projects with the Trivandrum [46,47], and Sakata projects [44,45] are examples of breakwater devices. In addition, the Mighty Whale is an offshore floating type [64]. These projects are necessary to the current understanding and improvement of W-T technology and in many cases serve as test beds and data collection tools.

Table II. Summary of the existing W-T projects.

Device	Location	Building	Output (kW)	Number of turbines	Diameter (m)	Type of turbine
Sanze shoreline gully	Gully, Japan	1984	40	2	NA	NA
Kvaerner-Brug, Norwegian OWC	Toftestallen, Norway	1985	500	1	NA	NA
Sakata, Japan	Sakata, Japan	1989	60	1	1.337	Monoplane with guide vanes
Prototype OWC device [212]	Islay, Scotland	1991	75	2	1.2	Biplane
Vizhinjam OWC	Trivandrum, India	1991	150	1	2	Monoplane
OSPREY	Dounreay, Scotland	1995	2,000	4	3	Contra-rotating
Mighty Whale	Japan	1998	120	1	1.7	Monoplane with guide vanes
The Pico Power Plant	Azores, Portugal	1999	400	1	2.3	Monoplane with guide vanes
LIMPET	Islay, Scotland	2000	500	2	2.6	Contra-rotating
Shanwei, Guangdong, China	Shanwei, Guangdong, China	2001	100	NA	NA	NA
Mutriku Wave Energy Plant [48,49]	Basque Country, Spain	2009	296	16	1.25	Biplane

Several studies have investigated the overall performance of W-T in existing shoreline installations with the aim of improving its efficiency. For example, the W-T prototype installed in Islay, Scotland is investigated in [65,66]. The Vizhinjam OWC was installed in Trivandrum, India in 1991 and is investigated in [67]. Numerical simulation of [67] shows an increase of turbine output power for a numerical module with control mechanism (by varying the rotor resistance of the induction machine) as compared with an uncontrolled one, for the same variation of differential pressure (aerodynamic input, N/m^2). The performance of the contra-rotating W-T installed in the LIMPET is compared with the predicted performance from theoretical analysis and model tests in [68]. It is found that a contra-rotating W-T has a lower efficiency than a biplane or monoplane W-T with guide vanes. In addition, a contra-rotating W-T requires an additional generator, or a gearbox.

3. PERFORMANCE PARAMETERS OF W-T

There are several factors that influence the design, hence performance, of W-T [6,16,69]. The optimization and improvement of such parameters aim mainly at overcoming the existing disadvantages of the system. Typical W-T systems show several well-known drawbacks: low tangential force, leading to low power output from the turbine; high undesired axial force; a relatively low aerodynamic efficiency; and a limited range of operation due to stall. This section of the article aims at reviewing the efforts performed to overcome such disadvantages and improve the performance by controlling the design parameters.

3.1. Guide vane

In a number of previous studies, it was concluded that the delay of stall onset contributes to improving W-T performance. This delay can be achieved by setting guide vanes on the rotor's hub as illustrated in Figure 4.

The variables that affect the aerodynamic performance of a W-T are discussed in [16,69], and it was found that the swirl losses at the turbine exit can be reduced by the use of guide vanes. Also, a multi-plane turbine without guide vanes was less efficient (approximately 20%) than the one with guide vanes. By testing a W-T model under steady flow conditions, and using the computer simulation (quasi-steady analysis), a comparison between W-Ts having 2D guide vanes and 3D guide vanes is conducted [70,71]. It showed that the 3D case has superior characteristics in the running and starting conditions. The results of mathematical simulations considering several aerodynamic designs of the W-T are shown in Table III [72]. Different guide vanes designs were compared and investigated analytically [73], taking into account the turbine starting characteristics and efficiency in irregular wave conditions. Table IV shows the best two designs, but for the total performance, R7N08N65 G15N11S40 is recommended. R7N08N65 has rectangular blades, a solidity of 0.7, normal blades, 8 blades, and a tip clearance (TC) (the gap between the casing and blade tip) of 0.65 mm. The G15N11S40 has 1.5 solidity, 11 blades, and the axial spacing between rotor and guide vane equals to 40 mm.

3.2. Hysteretic behavior

As shown in Figure 5, due to the reciprocating flow, the performance of the W-T has a hysteretic loop in which

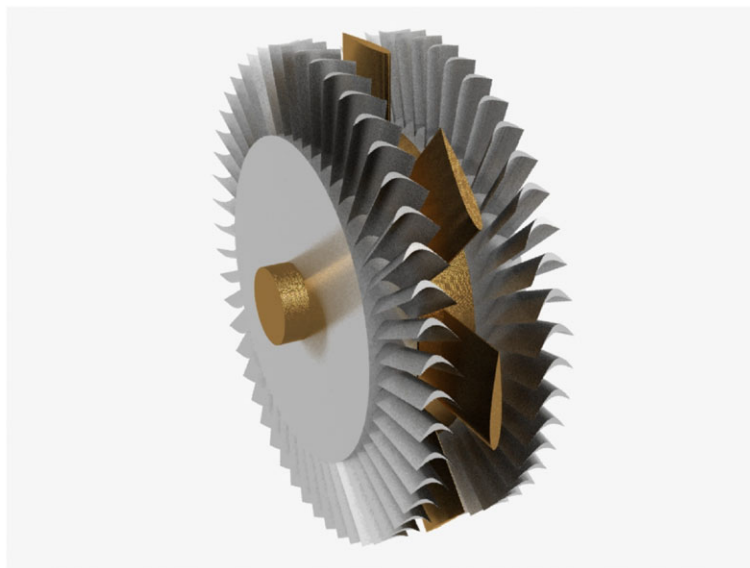


Figure 4. Illustration of guide vanes installed with W-T rotor.

Table III. A summary of the performance data for the different turbines [72].

Maximum efficiency	NACA0015 (%)		HSIM 15-262123-1576 [213] (%)	
	Without guide vanes	With guide vanes	Without guide vanes	with guide vanes
	58	71	55	67

Table IV. Maximum efficiency with minimum torque and starting torque coefficients [73].

Turbine profile	Maximum efficiency (%)	Minimum torque coefficient	Starting torque coefficient
R7N08N65 G15N11S40	44.8	0.41	0.49
R7N08F65 G15N21S31	47.4	0.08	0.33

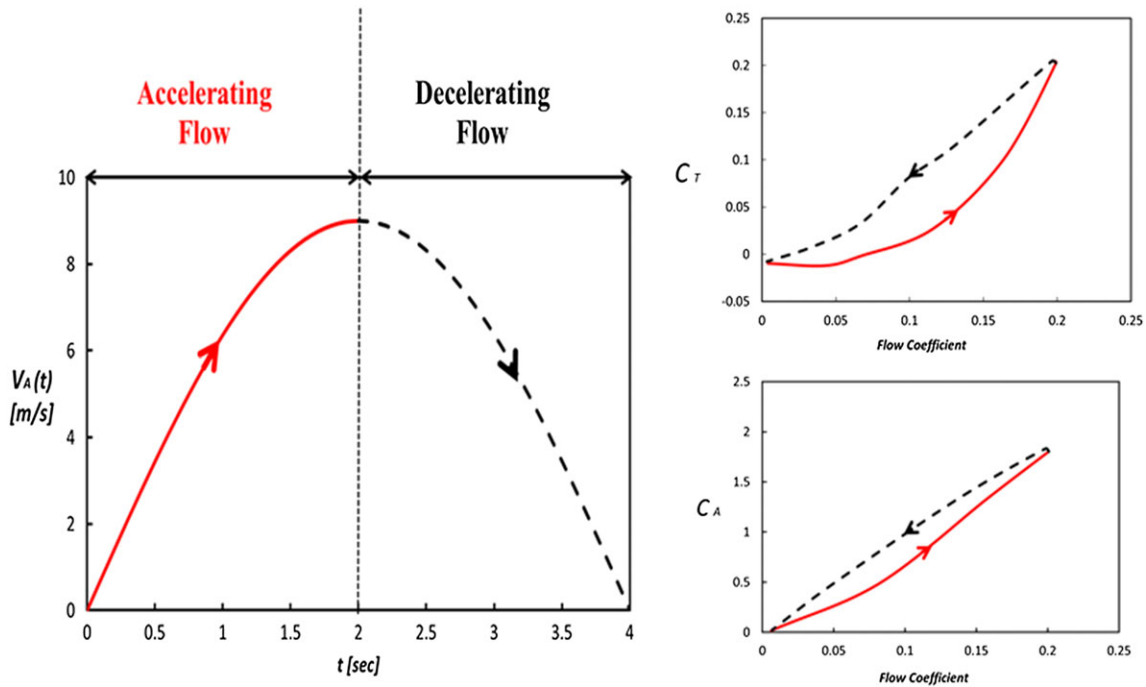


Figure 5. Typical hysteresis loop obtained in the W-T for one-half cycle of the sinusoidal flow in the unstalled condition. Graph reproduced after [4].

the values of C_A and C_T in the accelerating flow are smaller than those in the decelerating flow. Hysteresis characteristics are produced by the pressure difference induced by the different behavior of wakes between an accelerating flow and a decelerating flow in the same angle of attack, as illustrated in Figure 5.

A considerable number of parametric studies, using experimental and numerical approaches, are presented in [16]. It is found that the hysteresis effects are caused by asymmetry in the boundary-layer development on the blade surface and oscillating motion of the wake, the extent of which can be appreciable at low Reynolds numbers. Hysteresis effects are found to be directly proportional to the turbine solidity [16] and blade thickness [74] and insensitive to blade AR and surface roughness [74]. These effects can be smaller on large-scale turbines where the boundary layer on the blades is turbulent and relatively

thin. A CFD model of W-T is used to investigate the hysteretic behavior in [75]. The blade angle of attack is also found to be directly proportional to the hysteretic effects. In order to investigate the mechanism of the hysteretic behavior of W-T and also the effect of solidity, setting angles and blade thickness on the hysteretic behavior of W-T (where the setting angle is defined as an angle between the blade chord line and the rotational direction of rotor, ωR_m), CFD simulations are conducted for the flow field around a blade of a W-T by [76,77]. It is found that the mechanism to change the vortex intensity in the wake can be explained according to the vortex theorem. The vortex is intensified by the clockwise trailing shed vortices in the accelerating flow process, while it is suppressed by the counterclockwise vortices in the decelerating flow process. The hysteretic characteristics in sinusoidal flow are experimentally assessed in four kinds of

turbines (NACA0020; NACA0015; CA9; and HSM 15-262123-1576) in [78,79]. It is found that all turbines have similar hysteric loops; however, the hysteresis characteristics of the W-T are less sensitive to the blade profile than to solidity, setting angles, and blade thickness.

Numerical simulations are conducted for the hysteric behavior of monoplane and biplane W-Ts in [80–82]. It is found that for the monoplane W-T, the hysteric loop is opposite to the well-known dynamic stall [83–88] of an airfoil. The hysteric behavior is associated with a stream wise vertical flow appearing near the suction surface. For the biplane W-T, the hysteric behavior is similar to that of the monoplane at lower attack angles. However, the hysteric loop similar to the dynamic stall is observed at higher attack angles, which is attributed to unsteady flow separation near the hub and the trailing edge of the suction surface of the upstream blade. The magnitude of hysteric loop is further decreased in the biplane turbine with staggered blades than the one without stagger.

The effects of blade profile and rotor solidity on hysteric behavior of W-T operating under bidirectional airflow have been experimentally studied in [89,90]. It is shown that the size of hysteric loop of pressure coefficient greatly decreases with the reduction in rotor solidity. Such characteristics are less sensitive to blade profile, as shown in [78,79]. However, the effects of the TC region cause a reduction of the maximum torque coefficient and a decrease of the hysteric behavior [91]. The effects of unsteady flow conditions on the performance of a monoplane W-T without guide vanes during a field experiment on an OWC device are described in [92,93]. The torque coefficient shows a hysteric mechanism characterized by a counterclockwise loop that appears with high frequency oscillations. A dynamic stall phenomenon appears with oscillations of very large amplitude, independently from the frequency.

3.3. Multiplane W-T

For W-T systems that operate at high pressure values, a multiplane (usually tow stage) turbine configuration can be used. Such a concept avoids the use of guide vanes, and therefore, the turbine would require less maintenance and repairs [16]. The biplane W-T (Figure 6(a)) and the contra-rotating W-T (Figure 6(b)) are investigated to achieve this purpose.

The performance of a biplane W-T is dependent on the gap between the planes, as shown in [16]. A gap-to-chord ratio between the planes of 1.0 is recommended for the design of biplane W-T in order to achieve high efficiency in a limited space. A multi-plane turbine without guide vanes is less efficient than that with guide vanes but is relatively simple to design. A high solidity monoplane or a biplane W-T is a simple configuration but has large kinetic energy losses because of swirl at the exit. Experimental results in [94] show that the use of two twin rotors rotating in the opposite direction to each other is an

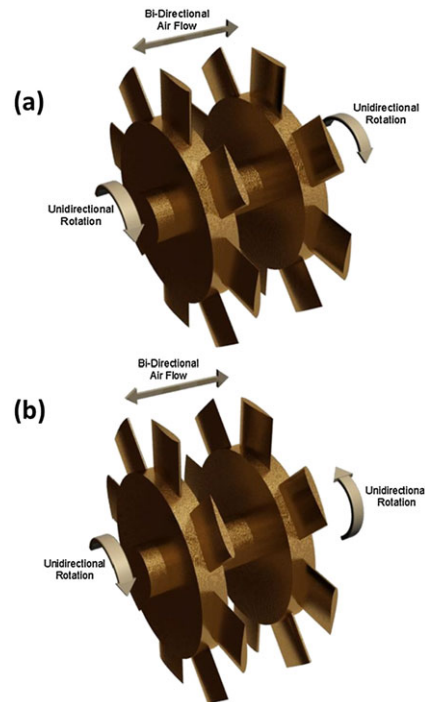


Figure 6. Multiplane W-T: (a) biplanes W-T and (b) contra-rotating W-T.

efficient means of recovering the swirl kinetic energy without the use of guide vanes.

The overall performance of several types of W-T design has been studied in [95] and by using a semi-empirical method for predicting the performance in [96]. Similar comparisons are undertaken using experimental measurement in [97]. Monoplane, biplane, monoplane with guide vane, and contra-rotating turbines viscous losses on the turbine rotors constitute the largest part of the losses. Therefore, the recovery methods have specific operational ranges. The contra-rotating turbine has an operational range that is similar to that of the monoplane turbine with guide vanes and achieves similar peak efficiency. However, the flow performs better than later in the post-stall region. The value of peak efficiency of contra-rotating turbine is higher than that of monoplane turbine without guide vane by 12% and by 9% for biplane turbine. It is also evident in [97] that the swirl component determines which rotor of a multi-plane turbine will stall first. On quite the contrary, investigated in [68] are used theoretical analysis and model tests to the predicted performance of the contra-rotating W-T installed in the LIMPET, and it is found that a contra-rotating W-T has a lower efficiency than that of a biplane or monoplane W-T with guide vanes. In addition, a contra-rotating W-T requires an additional generator, or a gearbox, to reverse the direction of rotation of one rotor.

Two-stage W-Ts with symmetric and non-symmetric airfoils have been investigated in [98]. Numerical optimization procedure has been carried out to optimize the

performance of the turbine as a function of the non-dimensional gap between the two rotors. It leads to an optimal value of the non-dimensional gap near 0.85 when simultaneously considering the request of maximum tangential force coefficient, of maximum efficiency for the prescribed operating range (angle of incidence = 8° to 14°) and the needed size of the system.

Detailed numerical analysis of biplane W-T performance has been performed in [99]. The downstream rotor curbs the turbine during start up and therefore delays its start up. Also, it produces 10%–30% of the total turbine torque and 40% of the total pressure drop during normal operation. The downstream rotor has an efficiency of 20%–60% of the upstream rotor efficiency during normal operation. Exergy analysis is also performed using the numerical simulation for steady state biplane W-Ts. The upstream rotor has a design second law efficiency of 82.3%, although compared with the downstream rotor second law efficiency of 60.7%.

3.4. Flow through W-T

It is important to design a turbine that has as high operating aerodynamic efficiency as possible and is matched with the OWC system for pressure drop and flow rate over a wide range of sea conditions. For this purpose, many studies have investigated the flow through the turbine, (Figure 7).

The basic principles and procedures for designing a W-T for a wave energy power station are described in [69]. The aerodynamic efficiency increases with flow ratio up to a certain critical value, after which it decreases. In order to avoid transonic effects, the maximum Mach number on the blades should be less than the critical Mach number. However, the critical Mach number decreases with an increase in incidence or solidity. Finally, the turbine maximum efficiency increases with an increase in Reynolds number.

The prediction methods and the variables that affect the aerodynamic performance of a W-T are reviewed in [16]. It shows that W-T is less sensitive to inlet turbulence compared with conventional turbo-machines. The performance

of a turbine in sinusoidal flow is better than that in a random air flow.

The use of CFD method to investigate the performance of a W-T is described in [100]. It is found that stalling of the flow does not occur first at the blade root and spread outward. It appears rather to be associated with the TC vortex and to spread inboard from the near-tip region.

A computational model has been used in [101] to study the performance and aerodynamics of the turbine, quantitatively and qualitatively. In addition, it is used to study the flow coefficient, turbine stalls and the appropriate inlet velocity profile. It is found from the computed results that the wakes behind the turbine blades (NACA0021) merge rigorously in the portion of Radius ratio (0.45:1.0), which leads the turbine to stall. The TC leakage flow is considerably higher in the trailing edge portion. However, as the flow coefficient increases, leakage flow region advances toward the leading edge, causing a large mass flow of air to leak through the gap.

The flow field through a high solidity ($\sigma = 0.6366$) W-T using blades with constant chord NACA0015 profiles is described in details in [37]. Separation at the outer radii has been detected for high values of the flow rate, which turns out to be induced by a radical shift of the mass flow through the turbine, mainly because of the cascade effect [29].

Numerical simulations have been performed to examine the flow field through the turbine blades at different flow rates in [36]. It is found that the flow separation at the tip is detectable by the presence of the pressure plateau along the suction side at coefficient equals to 0.238 and, more importantly, at coefficient equals to 0.257.

An analysis based on the actuator disk theory [102–104] is presented, and results are compared with corresponding CFD simulations in [38]. It is illustrated that for low values of flow coefficient, flow separation occurs near the rotor hub rather than at the blade tip, consequently improving the global turbine performance.

Numerical simulations are performed in [105] to indicate that pressure and torque coefficients increase when the flow rate coefficient increases. Highest calculated efficiency of the W-T in [105] is calculated to be around

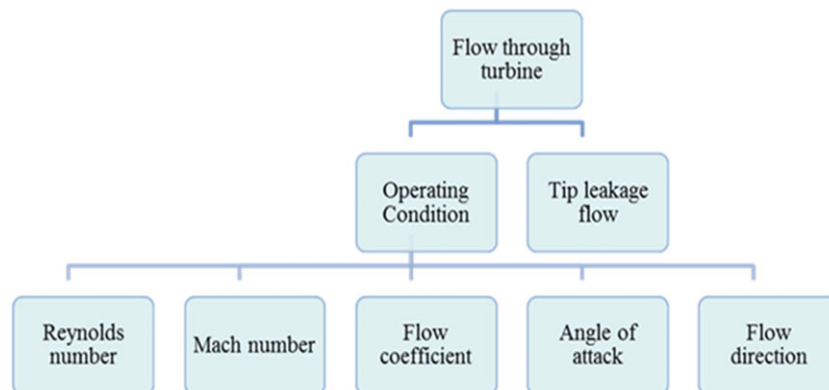


Figure 7. Flow over turbine parts and operating condition parameter.

60% for non-dimensional flow coefficient equals to 0.155. Operation of one OWC plant would produce 1850 kWh of energy per year for the assumed average sea regime data in the Adriatic Sea [106].

Experimental characterization of W-T with NACA0015 profiles submitted to a bidirectional flow is carried out, and the results are presented and analyzed in [107]. For several test conditions, the maximum efficiency (approximately from 0.3 to 0.43 for different test) of the turbine is always obtained for values of the flow coefficient between 0.19 and 0.21.

The entropy generation, due to viscous dissipation, around W-T has been recently examined by the authors in [108,109]. NACA0015 gives a less global entropy generation rate and a higher efficiency rate compared with other airfoils. From the study of the behavior of four different airfoils, NACA0015 is not the best airfoil in all conditions. For example, at maximum Reynolds number, NACA0012 gives a less global entropy generation rate, and NACA0020 creates the minimum value, so it is a good concept to create an optimum design airfoil that gives better results than NACA0015. This study suggests possible existence of critical Reynolds number at which a viscous irreversibility takes minimum values.

3.5. Design optimization

This subsection reviews different methods to optimize the design of W-T in order to improve its overall performance: by changing in blade dimension or position, by adding plate on the blade, or finally by creating a new blade shape (Figure 8).

3.5.1. Different design parameter for turbine

Various wind tunnel tests on NACA four-digit airfoils in a tandem cascade with the angles of incidence ranging from 0° to 90° are described in [29]. The increase in the blade thickness results in larger negative values of torque coefficient and has a favorable effect on starting.

The prediction methods and the variables that affect the aerodynamic performance of a W-T are discussed in [16,69]. A large solidity is needed for the turbine to be self-starting. It is advisable to choose a thicker profile for small-scale turbines and a thinner profile for a large-scale turbine. Values of hub-to-tip ratio approximately equal to 0.6 are recommended for design.

The ability of a 3D CFD method to predict the effect of solidity on the performance of a monoplane W-T has been tested by [110]. Calculations of the effect of solidity on turbine performance are predicted both qualitatively and quantitatively, and the effect of clearance is qualitatively correct.

The operational matching of the performance of the turbine is used as the premise in achieving an optimal design configuration and sizing. The range and frequency of power bands presented to the turbine over long periods of time are in [111], which results in a 5% improvement in power output with the optimal size of the turbine

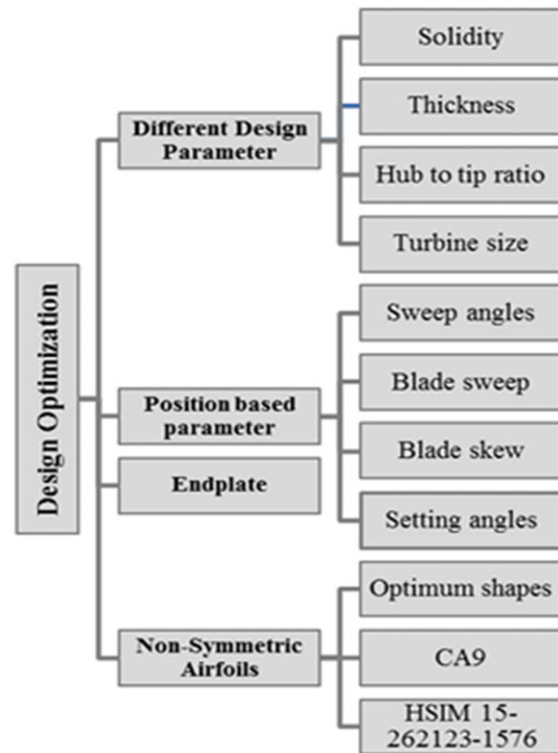


Figure 8. Design optimization parameter and sub parameter.

required to be slightly larger than the average pneumatic power rating would suggest.

3.5.2. Position based parameter

The change in the position of blade according to the hub centerline through different parameters (sweep angle, blade sweep, blade skew, and setting angles) has a direct effect on the performance of turbine.

3.5.2.1. Sweep angle, blade sweep, and blade skew.

An experimental work is presented to investigate and compare the aerodynamic performance of the backward swept, see Figure 9(a), and unswept angle blades for different rotor solidities (0.64 and 0.32) for 0° and 20° setting pitch angles in [112]. Results for the 0° setting pitch angles have shown that the swept back angle blade produces a more positive value of efficiency and torque than that of the standard unswept blades but at the expense of peak efficiency. The experimental results show that this sweeping back angle has to be minimized in order to reduce its detrimental effect on the overall turbine efficiency.

The calculations of the blade sweeps for the W-T, see Figure 9(b), with a numerical code by [113] and experimentally with quasi-steady analysis in [79]. As a result, it is found that the performance of the W-Ts is influenced by the blade sweep, and a suitable choice for the sweep ratio is 35%.

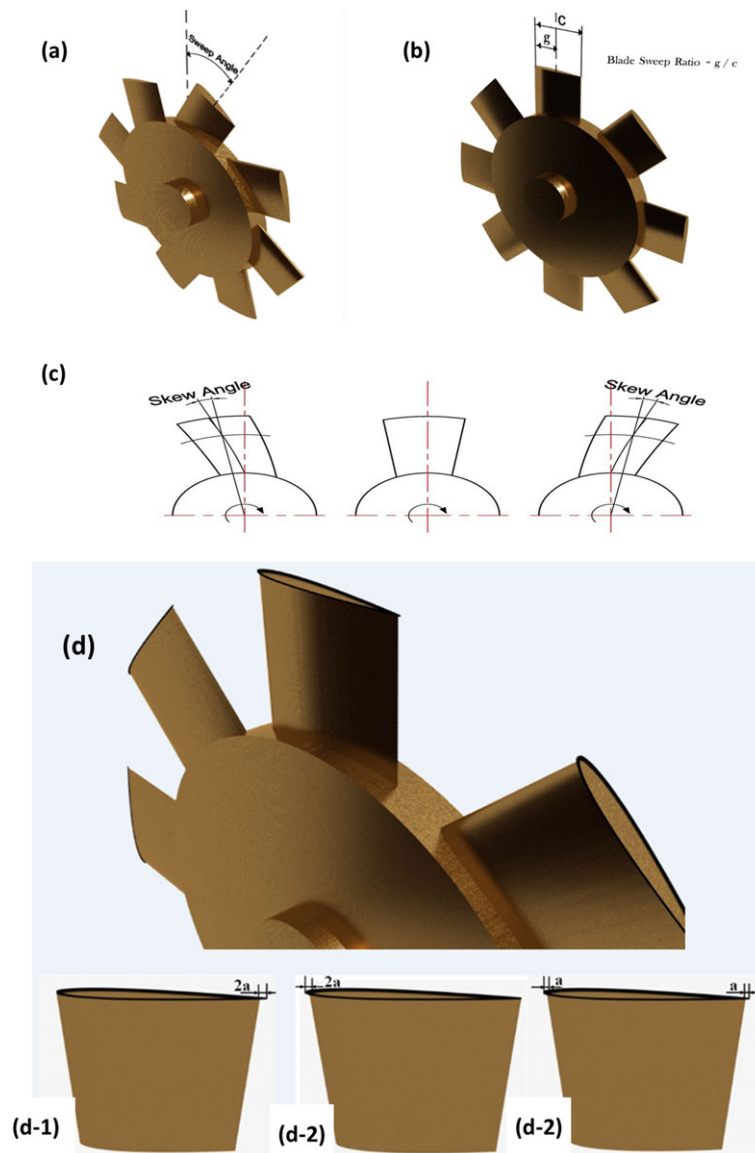


Figure 9. Position-based parameter: (a) backward sweep angle; (b) blade sweep ratio; (c) blade skew (left: backward skewed blade; middle: straight blade; right: forward skewed blade) [114]; and (d) rotor blade with end plate (d-1) backward type and (d-2) forward type (d-3) middle type.

The effect of blade skew, see Figure 9(c), on the aerodynamic performance and associated aerodynamic noise is assessed in [114] by using both numerical simulations and experiments to develop an analytical blade design tool for W-Ts, incorporating blade skew. Inception of stall inevitably causes an increase of specific sound power level by up to 20 dB. The backward/forward blade skew delays the onset of stall and extends the turbine's range of stall-free operation by 106% of the baseline. The flow generated sound in unstalled operation was decreased up to 3 dB by optimal backward/forward blade skew.

3.5.2.2. Setting pitch angles for blade. Setting the blades at their optimum pitch angle during compression

and suction is expected to substantially improve W-T efficiency [115–122]. This is achieved by the turbine manufacturer in such a way to allow the turbine blades to rotate around their axis with an angle that equals \pm optimum blade setting pitch angle.

The performance of W-T using self-pitch-controlled blades taking real air flows to the turbine into account is clarified by [123]. Experimental investigations and computer simulations using a quasi-steady analysis are performed on the optimum setting angle during suction, and it is found to be 6° while the one during compression is found to be 10° .

A modified W-T with setting angle has been investigated by model testing and numerical simulation in

[124]. It is found that the new turbine using rotor blades with a fixed setting angle is superior to the conventional W-T and that the optimum setting angle was 2° for compression velocity amplitude to suction velocity ratios 0.8 and 0.6, in both with guide vanes and without guide vanes configurations.

A 400-kw variable-pitch W-T is built to be tested in the Pico plant, Azores, Portugal alongside a fixed-pitch W-T of a similar rating [125]. It is hoped that the variable-pitch W-T will demonstrate increased net energy productivity. Therefore, the variable-pitch turbine should be able to demonstrate increased energy productivity compared with that of fixed-pitch machines. Moreover, the eddy-current pitch actuation system should provide responsive and energy efficient pitching, but it was never installed. The relatively modest efficiency of the W-T, especially when operating in the compressor mode, severely limits the gains from reactive control.

A numerical optimization algorithm based on CFD simulation is implemented in order to optimize the blade pitch angle in [126]. The standard NACA 0021 and an optimized profile (AOP) are numerically investigated. The present CFD optimization results show that the optimum blade pitch angle for NACA 0021 is $+0.3^\circ$ while that of the AOP equals $+0.6^\circ$. The present airfoils with the optimized pitch angle show an average efficiency improvement of 3.4% for standard NACA 0021 and 4.3% for the AOP.

A numerical optimization algorithm is implemented in this work [127]. The present CFD optimization results show that the optimum blade pitch angle for NACA 0021 is 0.3° while that of the optimized blade equals 0.6° . Up to 2.3% improvement in NACA 0021 turbine efficiency and 6.2% improvement in AOP efficiency are achieved.

3.5.3. End plate

In order to improve the performance of the W-T, the effect of end plate, see Figure 9(d), on the turbine characteristics has been examined in [128,129]. Using an experimental model and CFD method show that the optimum plate position was a forward type (Figure 9(d-2)). Also, the peak efficiency increases approximately 4% as compared with the W-T without an end plate.

3.5.4. Non-symmetric airfoils

A methodology for numerical simulation of a CA9 rotor W-T is presented in [130]. Researchers have stressed the use of traditional symmetrical NACA series blades until they developed AOPs: CA9, which has the same thickness as NACA0015 and is optimized in terms of the leading edge radius, maximum thickness position, and trailing edge slope [131,132]. It shows superiority over a standard NACA0015. A maximum efficiency of 70% is obtained, and the overall computed performance related to reasonable qualitative agreement with experimental one.

The calculations of the blade sweeps for the W-T with the NACA0020 and the CA9 blades are carried out to clarify the performance with a numerical code by [113]. The overall performances for the NACA0020 blade are

better than those for the CA9 blade. Generally, the blade thickness is thinner on NACA four-digit series, while the maximum efficiency is higher, and the stall margin deteriorates. However, both the maximum efficiency and the stall margin for the NACA0020 blade in this calculation are better related to those for the CA9 blade.

Four kinds of blade profile are selected with regard to the blade profile of the W-T in [78,79,133]. The types of blade profiles are as follows: NACA0020, NACA0015, CA9, and HSIM 15-262123-1576. The experimental investigations have been performed for two solidities (0.48 and 0.64) by experimental testing (steady flow conditions) and numerical simulation using a quasi-steady analysis (running and starting characteristics under sinusoidal flow). As a conclusion, NACA0020 is superior to other turbines (NACA0020; NACA0015; CA9; and HSIM 15-262123-1576) in the small-scale model testing. For a large-scale W-T operated at high Reynolds number, a suitable choice is the blade profile of NACA0015. However, the experimental investigations operating under sinusoidal and real sea conditions in [89,90] conclude that the preferred rotor geometry is CA9 blade profile, with rotor solidity 0.64.

Two-stage W-Ts with symmetric and non-symmetric airfoils have been investigated in [98], and the numerical algorithms are used to estimate the optimum shape with an increase of efficiency (by 2.1%) and of tangential force coefficient (by 6%), compared with the standard NACA 2421. An optimization process is employed in order to increase the tangential force induced by a monoplane W-T in [134]. A relative increase of the tangential force coefficient exceeding 8.8% (as a mean, 11.3%) is obtained for the full operating range. At the same time, the efficiency improves also by at least 0.2% and up to 3.2% (as a mean, 1%) compared with the standard NACA 0021.

A comparison of total entropy generation, due to viscous dissipation, between a suggested design (variable chord) and a constant chord W-T is presented in [135]. The detailed results demonstrate an increase in static pressure difference around new blade and a 26.02% average decrease in total entropy generation throughout the full operating range.

3.6. Tip clearance

The gap between the casing and blade tip is a very effective parameter on the turbine behavior. The effect of the flow around the tip is more significant in the process of turbine stall than that around the hub [136–138].

The prediction methods and the variables that affect the aerodynamic performance of a W-T are discussed in [16,69]. The W-T is very sensitive to TC when compared with conventional turbines. Therefore, values of a TC ratio less than 0.02 are recommended for design.

The ability of a 3D CFD method to predict the effect of TC on the performance of a monoplane W-T has been tested in [110]. It is shown that as the TC increases, the performance of the turbine drops.

In order to examine the effect of the extent of the TC on the steady performance of the turbine, the results of

numerical computations performed with different TC (1%, 5%, and 10% of the chord length) and different flow conditions (0.15, 0.225, and 0.275) are illustrated in [37]. The stagnation pressure drop coefficient decreases when increasing the TC. On the other hand, the torque coefficient decreases when increasing the TC. In fact, the gap must be neither too small in order to avoid flow separation already existing at low values of the flow coefficient nor too large in order to avoid too small performance caused by small pressure drop through the turbine and large tip leakage flow.

A comparison between numerical and experimental investigations is conducted in [139] for studying uniform TC ratio. Regarding turbine efficiency, it is found that the peak efficiency of the turbine decreases and shifts toward a higher flow coefficient as the TC to chord length ratio increases, while the stall margin becomes wider.

The performance of a W-T with various non-uniform TC is examined using CFD by [140]. The performance of turbines with uniform and non-uniform TC is compared. It is shown that the turbine with non-uniform TC seems to have a preferable overall performance.

CFD models based on the LIMPET OWC turbo generation section are studied in [141] to investigate how airflow impingement created by a rotating turbine directly upstream increases the heat transfer away from an electrical generator, and also how this could be increased by adjusting the clearance between the turbine tips and shroud. As the clearance between the turbine tip and shroud is reduced, the performance of the turbine in terms of torque and efficiency rises as does the heat transfer from the generator.

3.7. Other variables' effect on overall performance

In order to enhance the overall performance of W-T systems, different parameters such as turbine material, mechanics of materials, oscillating chamber, and the electricity generation in the system are also investigated.

3.7.1. Materials and mechanics of materials

The selection of materials for airfoil blades component is one of the most important issues in the optimum design of W-T employed in an OWC wave power generator as shown in [142]. The selection of materials using Cambridge materials selector [143] and simple tabulation has separated and ranked five candidates out of 167 materials class, consisting of Titanium alloys class, GFRP class, and CFRP class. Further evaluation has specified two prime candidates: Fiber Reinforced Composites (Carbon Fiber/Epoxy Resin) and Titanium Alloys (Ti6Al4V).

The authors in [144] describe the methods developed during the design and development phase of its W-T suitable for installation into active renewable energy breakwater schemes. Due to the bespoke nature of the systems involved, a finite element analysis is implemented to stress critical components. This piece of information is fed into fatigue analysis routines for component life estimation. The

loading, geometry, and material models are combined to create a fatigue life prediction. The stresses are then added together to give a total stress. The total annual contribution to fatigue from the wave loading is found. This fatigue damage is combined with the damage created from the start–stop cycles to give an overall fatigue life prediction of 44 years.

3.7.2. Oscillating chamber

With an additional vertical duct at the wave-beaten side in the of house OWC system, it is expected to give some better performances in [145]. It can be concluded that a U-OWC can give performances better than those of a conventional OWC both with swells and large wind waves. Furthermore, a U-OWC can give performances better than those of a conventional OWC also with small wind waves. In heavy sea states, the conventional OWC is expected to suck air through the opening in the wave-beaten wall, for some short span of time; not so the U-OWC. Under the same weight, a breakwater embodying the U-OWC has a safety factor slightly greater than the safety factor of a breakwater embodying the conventional OWC.

The effects of duct area ratio and duct angle are examined in order to optimize W-T performance in [146]. The turbine performance is numerically investigated by CFD models. The duct area ratio equals to 1.5 is considered the optimum area ratio for the investigated turbine as a maximum value of 10% increase of the turbine power is achieved. Increasing the duct angle to an optimum value of 7° at this optimum duct area ratio ensures separation free flow in the downstream diffuser and up to 14% improvement in turbine power and up to 9% increase of the turbine efficiency.

3.7.3. Electricity generation

Two control strategies of an OWC-W-T generator module are proposed and compared in order to study the stalling behavior in the W-T by [41]. In the first one, a rotational speed control system is employed to appropriately adapt the speed of the double-fed induction generator coupling to the turbine, according to the pressure drop entry. In the second control strategy, an airflow control regulates the power generated by the turbine generator module by means of the modulation valve avoiding the stalling behavior. The experiments suggest that the air control valve is more adequate to regulate the generated power according to the demand of the grid. Therefore, the obtained results depict the ability of both methods to control the generated active power fed to the grid in ways that may complement each other.

4. W-T COMPARISONS AND CONNECTIONS WITH OTHER TURBINES

Many kinds of self-rectifying air turbines that have improved over the decades are proposed [23,115,147–154]. However, a comparison of all of these characteristics

has yet to be made. The types of turbines are summarized as follows in Table V:

The characteristics of several types of W-T for wave power conversion proposed so far have been investigated by experimental measurements and numerical simulation under irregular flow conditions in [20,155] at Saga University, see Table VI. It has been found that the impulse type turbines have the potential to be superior to the W-T in overall performances under irregular flow conditions, see Figure 10(a). Non-dimensional performance curves of the turbines are obtained from model testing, based on the stochastic analysis of the OWC spar buoy wave energy converter in an offshore wave climate [156]. In the simulations, the converter is equipped with various types and sizes of self-rectifying air turbines, namely single-stage and multi-stage W-T and new biradial-impulse turbines [157,158]. The results demonstrate that several (possibly four) stages are required for acceptable performance (67% efficiency), if a W-T is to be adopted. The new biradial-impulse turbine was found to exhibit an overall device performance (71% efficiency) better than that of the multi-stage W-T, with the advantage of a substantially smaller rotor diameter without the need for several stages, see Figure 10(b).

An impulse with fixed guide vanes turbine for bidirectional flow is used as the booster turbine in order to improve the efficiency of W-T at high flow coefficient by [26]. The energy from oscillating airflow was captured by W-T at low flow coefficient and the impulse turbine acquires the energy at high flow coefficient. The performances of axial

flow turbines under steady flow conditions have been investigated experimentally by model testing. Furthermore, the mean efficiency of the turbine is estimated by quasi-steady analysis in this study. The mean efficiency of the turbine strongly depends on turbine diameter ratio. The mean efficiency at high flow coefficient is improved by means of the impulse turbine as a booster turbine and the peak mean efficiency is lower than that of a single turbine. It can be concluded that it is a new approach to use two different turbines in one system in order to avoid the disadvantages of both turbines.

5. COMPUTATIONAL FLUID DYNAMICS MODELS OF W-T

5.1. General description of the flow around W-T

To the best of the authors' knowledge, there are no published studies about the physics of oscillating flow around W-T using laser techniques. It is difficult, therefore, to correlate the published CFD models of such flow physics in order to induce a universally valid description of all flow phenomena. However, there are some phenomena that do exist because of the nature of the oscillating flow behavior as well as to the operational structure of the turbine. There are numerous experimental studies that were conducted using high-resolution measurement techniques, which studied oscillating flow (i.e., oscillating angle of attack) around stationary and moving airfoil for aeronautic

Table V. Self-rectifying air turbines for wave energy conversion.

Type	Remarks
1	The W-T
1-A	W-T with guide vanes [214–216] It was adopted for the project "Mighty Whale" organized by JMSTEC, Japan [64,217].
1-B	W-T with self-pitch-controlled blades [115,119,149] The turbine blades can oscillate between two setting angles by themselves according to the flow direction, where the turbine has active pitch controlled blades [218].
1-C	Biplane W-T with guide vanes [219] This type is making progress in Islay, UK [218], where guide vanes are not used for the turbine.
1-D	Contra-rotating W-T [16,220] This is installed in the LIMPET system in Islay, UK [51,221], which is the world's first commercial wave power station.
2	Impulse turbine
2-A	Impulse turbine with self-pitch-controlled guide vanes [153,154] This turbine has been constructed by NIOT, India [222].
2-B	Impulse turbine with fixed guide vanes [23] This is being planned to be constructed in India, China, Korea, and Ireland [223].
2-C	McCormick counter-rotating turbine [224] The prototype model of the McCormick turbine was constructed and tested [150]. The disadvantage may be the balance of the gearing cost, and its noise generation may be a severe problem at specific sites.
3	Radial turbine [151,152] According to recent research, the efficiency is not so good [225].
4	Cross flow turbine and Savonius turbine [148] In order to obtain some fundamental data for the turbines, tests were performed under steady flow conditions [147]. However, in general, they are inferior to W-T type in their starting and running characteristics [226].

Table VI. Comparison between different turbines.

Turbine	Diameter (m)	Maximum efficiency under irregular flow condition (sea-state) (%)
Impulse turbine with self-pitch-controlled guide vanes	0.298	47
W-T with guide vanes	0.298	32
Impulse turbine with fixed guide vanes	0.298	38
W-T with self-pitch-controlled blades	0.298	45
Biplane W-T with guide vanes	0.298	34

applications. Such a flow is similar to the oscillating flow around W-T in the sense of the relationship between oscillating flow interaction with airfoil wall. For a NACA-0012 airfoil subjected to an oscillating flow of frequency 1.67 Hz at an average Reynolds number of 12×10^3 , it is found that the flow exhibits manifested vortical flow patterns [159]. Such a study is conducted using Laser Doppler Velocimetry and reports the presence of axial flow along the core of the vortices pattern, which complicates the

vorticity field. Similar flow patterns for the same airfoil are reported for a higher range of Reynolds number ($Re = 10^5 \sim 2 \times 10^5$) and lower frequency (0.188 Hz) [160]. Hribernik *et al.* [161] demonstrated by particle image velocimetry (PIV) measurements that the separation region (i.e., bubble) generated on a generic airfoil exhibits oscillations under oscillating angle of attack flow. They reported that the separation bubble oscillated around its mean position at an interval of 10% of the chord length. A similar oscillating behavior of the separation bubble was reported using Laser Doppler Velocimetry measurements, and correlated to dynamic stall conditions of a NACA0012 oscillating airfoil [162]. It was also reported that the flow near the leading edge wall, due to the oscillation of the separation bubble, changes from a jet-like flow to a wake flow. These results were recently confirmed in [163] using particle image velocimetry measurements of the flow around oscillating NACA0015 airfoil for Reynolds number of 2×10^5 and frequency of up to 0.5 Hz.

It is clear that the oscillating flow around W-T is complex. The presence of strong vorticity field, as well as the dynamic behavior of separation regions, can be easily confirmed by induction of similar flow phenomena in the absence of laser measurements of such flows in the time being. Streamline curvature around W-T was also

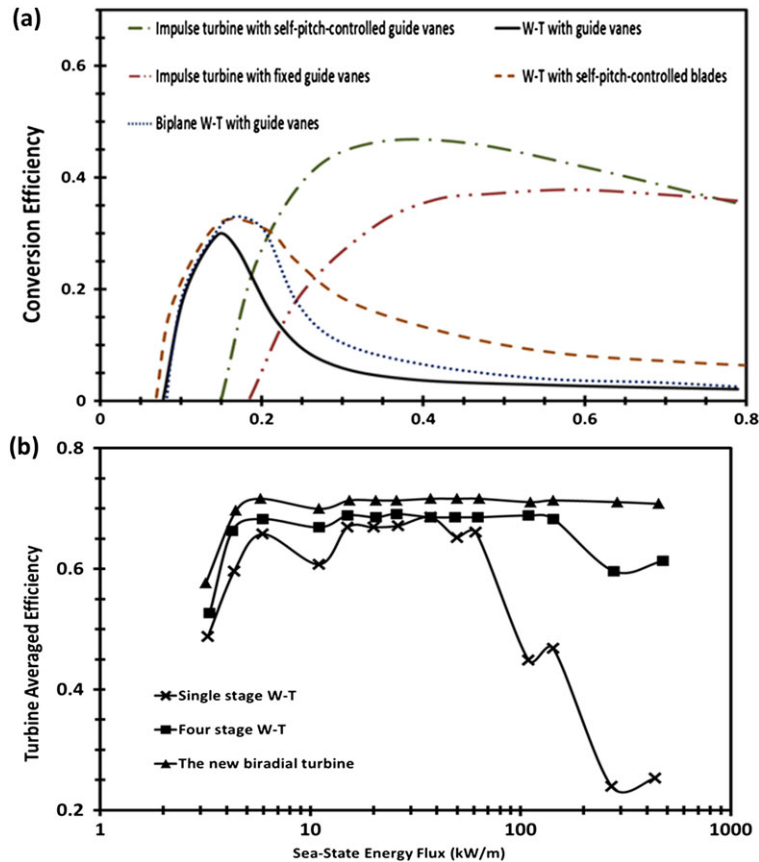


Figure 10. W-T comparisons with other turbines: (a) comparison of conversion efficiency of wave energy under irregular flow condition [20,155] and (b) turbine averaged efficiency versus sea-state energy flux for single/four stages W-T and for the new biradial turbine [156].

reported by means of numerical simulations [164]. These flow features impose certain critical limitations on the CFD models of W-T, especially in terms of modeled boundary conditions and turbulence models.

5.2. CFD modeling goals of W-T

Given the general operating conditions, air flow around and through W-T can generally be considered an incompressible flow. The Navier–Stokes equation, in conservation form, can be written as

$$\rho \frac{\partial u_i}{\partial t} + \rho \frac{\partial}{\partial x_j} (u_j u_i) = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} (2\mu s_{ji}) \quad (4)$$

where the strain rate tensor is $S_{ji} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$.

The modeling of turbulent flow through W-T can be performed by solving equation (31) directly on a computational grid with a number of cells in the order of $Re^{\frac{3}{4}}$ [165], which is computationally expensive if one considers rotor optimization simulations. The other two approaches, which are computationally efficient, are either by solving the Reynolds-averaged Navier–Stokes (RANS) using a Reynolds stress closure or by solving a filtered Navier–Stokes equation, or by using a hybrid approach that combines the previous two. A discussion of such approaches is presented in Section 5.3.

In fact, it is always difficult to decide which turbulence modeling approach to follow in CFD models. However, the consideration of the model essential objectives can be an excellent guideline to make such a decision. The ideal W-T CFD model objectives can be summarized as follows:

1. To provide good prediction of the flow around the turbine so that the performance parameters (such as forces, torque, and efficiency) can be computed.
2. To respond effectively to the changes in the design (i.e., flow geometry) so that different designs can be simulated for optimization purposes.

When these objectives are considered, the first issue to be discussed is model temporality. A large number of W-T CFD models relied on solutions of the steady averaged Navier–Stokes equation [37,113,139,140]. However, such models are only capable of providing average estimations of the turbine cycle relative to OWC. Models based on the unsteady solution of Navier–Stokes equation are numerous as well, mainly adopting uniform (i.e., sinusoidal) wave form on the boundary as an approximation of the irregular wave forms that exist in nature [90,166,167]. Models based on irregular wave forms are relatively scarce in literature records [168,169], perhaps because of the complexity that irregular boundary conditions impose on the model solution convergence. The use of steady models can be acceptable for preliminary achievement of the first modeling objective. However, given the numerous design details, as shown in Sections 3 and 4, and their impact on the flow structure, the use of

unsteady models is necessary to complete the first objective, and also the second one. Conservative sinusoidal approximation of irregular wave forms can be accepted for comparing design modifications or different components between two systems. Conservativeness in this context refers to precautions related to the averaging of the frequencies, not just the amplitudes, of the complete irregular wave spectrum. However, to use CFD as a tool for econometric analysis of Wells energy systems, models based on irregular wave forms that emulate the actual wave properties in the potential installation sites should be considered.

5.3. Turbulence modeling considerations

The solution of equation (31) in the turbulent flow regime requires an approach for modeling the high nonlinearity arising in the viscous term of the equation. The adoption of Reynolds averaging, which yields the RANS equation, is the most common approach for such purpose. The RANS equation is

$$\rho \frac{\partial U_i}{\partial t} + \rho U_j \frac{\partial U_i}{\partial x_j} = -\frac{\partial P}{\partial x_i} + \frac{\partial}{\partial x_j} \left(2\mu S_{ji} - \overline{\rho u_j u_i} \right) \quad (5)$$

The last term on the RANS of equation (5) is called the Reynolds stress term, often denoted as τ_{ji} . This term couples the turbulent fluctuations to the mean flow by assuming that such fluctuations generate additional stresses or produce momentum transport [170]. This term is the major problem of turbulence modeling because it requires to be solved in order to compute the mean flow field variables. However, to compute this term, additional equations are required. There are two major methods to provide closure for the Reynolds stress terms in the Navier–Stokes equation, as fully described in [171] and [170]. The first method is by taking the moments of the Navier–Stokes equation. This is achieved by multiplying the equation by a fluctuating property and performs time averaging for the resulting equation [171]. This method leads to the development of second order closures, which include transport equations for all the components of the Reynolds stress term. This is called Reynolds Stress Model. The most common and well-tested form of such model is the Launder, Reece, and Rodi model that was proposed in [172]. The model is composed of one transport equation for τ_{ji} , dissipation rate and pressure-strain correlations, auxiliary relation for the production of τ_{ji} and model coefficients [173]. Although such a model predicts the anisotropic flow field by calculating the components of τ_{ji} , its numerical implementation always faces numerous challenges that make the results of such a model not as accurate as they are theoretically expected. These challenges are thoroughly discussed in [174].

The second method of closure for the Reynolds stress term is the eddy viscosity concept. This concept is based on the work of Boussinesq who postulated that the momentum transfer caused by turbulent eddies is

analogous to the momentum transfer caused by the random motion of molecules [175]. A detailed explanation of the Boussinesq hypothesis is given in [171] and in a recent historical discussion presented in [176]. The Boussinesq hypothesis dictates that the Reynolds stress is proportional to the mean strain-rate tensor and the constant of proportionality is the turbulence or eddy viscosity a scalar quantity often denoted as (μ_T). According to such hypothesis, the Reynolds stress term is given by

$$-\overline{\rho u_i u_j} = \mu_t \left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) - \frac{2}{3} \delta_{ij} \left(\rho k + \mu_t \frac{\partial \bar{u}_k}{\partial x_k} \right) \quad (6)$$

The most common turbulence models for engineering applications are based on the eddy viscosity concept. It will be shown later in Section 5.4 that eddy viscosity models are the most common class of turbulence models used in modeling W-T. The following section explains some details about these models and their inherited physical assumptions.

5.3.1. Turbulent viscosity models

In order to solve equations (5) and (6), additional transport equations for calculating the turbulence scalars (i.e., turbulence kinetic energy and turbulence dissipation rate) must be solved. There are numerous models for different classes of turbulence flow that solve transport equations for such scalars. Each of these models has inherited physical assumptions that postulate limitations and restrictions on its implementation. The most commonly used turbulence models in the CFD models of W-T are the $k-\varepsilon$ models and $k-\omega$ models. The transport equations for such models can be found in [173]. Each class of these models computes turbulent viscosity via a specific scalar correlation. The following table (Table VII) shows different correlations for the most used eddy viscosity and the variables of each correlation.

Turbulent viscosity models are based on the assumption of isotropic turbulence, which means that these models inherently assume that the components of Reynolds stress tensor equally affect the mean flow in space. This assumption is coherent with Kolmogorov (1941) theory of turbulence [177,178]. Hence, although the isotropy assumption might lead to an intuition that turbulence viscosity predictions should not be accurate, extensive numerical

investigations utilizing these models have yielded successful predictions of complex flows. Examples on the success of eddy viscosity models in predicting different types of vorticity-dominated flow and flow with streamline curvature can be found in [179–190]. LES [191] provides an alternative approach in which the large eddies are computed in a time-dependent simulation that uses a set of filtered equations. Filtering is essentially a manipulation of the exact Navier–Stokes equations to remove only the eddies that are smaller than the size of the filter, which is usually taken as the mesh size. Like Reynolds averaging, the filtering process creates additional unknown terms that must be modeled in order to achieve closure. Statistics of the mean flow quantities, which are generally of most engineering interest, are gathered during the time-dependent simulation. The attraction of LES is that by modeling less of the turbulence (and solving more), the error induced by the turbulence model will be reduced [192].

It is theoretically possible to directly resolve the whole spectrum of turbulent scales using an approach known as DNS [193]. Basically, in LES, large eddies are resolved directly while small eddies are modeled. Solving only for the large eddies and modeling the smaller scales results in mesh resolution requirements that are much less restrictive than with DNS. Typically, mesh sizes can be at least one order of magnitude smaller than with DNS [194]. Furthermore, the time step sizes will be proportional to the eddy-turnover time, which is much less restrictive than with DNS. In practical terms, however, extremely fine meshes are still required. It is only due to the explosive increase in computer powers that LES can be considered as a possibility for engineering calculations [195,196]. However, the use of different turbulence models in W-T models requires certain considerations to be made. Some of these considerations are related to the empirical coefficients in the eddy viscosity and turbulence transport equations [197,198]. Other considerations are related to the suitability of each model to different flow regimes and configurations [199,200].

5.4. Review of CFD studies of W-T

Figure 11(a)–(c) highlight the importance of the CFD method in investigation the studies of the W-T improvement.

Table VII. Eddy viscosity correlation for the most used turbulence models in the W-T CFD models.

Eddy viscosity correlation	Turbulence model	Note
$\mu_t = \rho C_\mu \frac{k^2}{\varepsilon}$	Standard [227] and RNG [228] $k-\varepsilon$	C_μ is an empirical constant, and k and ε are the turbulence kinetic energy and its dissipation rate, respectively. C_μ values are 0.09 and 0.0845 for the standard and RNG models, respectively.
	Realizable $k-\varepsilon$ [229]	where C_μ is not constant and given by $C_\mu = \frac{1}{A_0 + A_1 U^* \frac{k}{\varepsilon}}$, where $A_0 = 4.0$; $U^* = \sqrt{S_{ij} S_{ij} + \Omega_{ij} \Omega_{ij}}$, $A_1 = \sqrt{6} \cos\left(\frac{1}{3} \arccos\left(\frac{\sqrt{6} W}{3}\right)\right)$, $W = \frac{\sqrt{8} S_{ij} S_{ij} S_{kl}}{S^3}$, and the vorticity tensor is given by $\Omega_{ij} = \frac{1}{2} \left(\frac{\partial \bar{u}_i}{\partial x_j} - \frac{\partial \bar{u}_j}{\partial x_i} \right)$
$\mu_T = \rho \frac{k}{\omega}$	Wilcox original [230] and modified [173] $k-\omega$	ω is the specific dissipation rate of turbulence kinetic energy

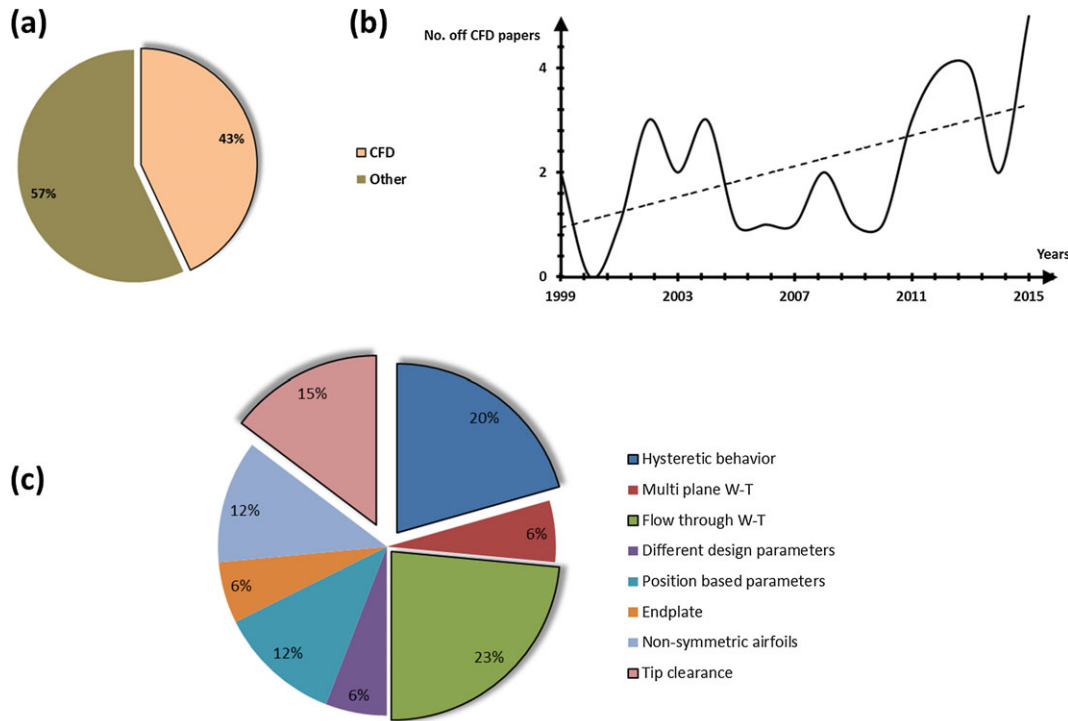


Figure 11. Review of CFD studies of W-T: (a) the percentage of use to CFD versus with other methods, (b) the number of CFD papers in different time period, and (c) the percentage of use to CFD in all point of research.

Figure 11(a) shows a classification of W-T research literature based on the methodology used in each study. It can be conceived that approximately 43% of the works used CFD models. Hence, a numerical model using the CFD code can be employed successfully to calculate the performance characteristics of W-T as well as the other methods (such as experimental and analytical). In addition, a number of CFD papers from 1999 to present are introduced in Figure 11(b). The increase of CFD papers (especially in the last 5 years) indicates that trend, with large proportion, to depend on the CFD method. Finally, the CFD works are quantitatively categorized in Figure 11(c). The hysteretic behavior, flow through turbine and TC, has the largest share of CFD modeling works. Due to the difficulty and the high cost of other methods, such as the experimental method, to make bidirectional flow with different operating conditions to study the flow of the hysteretic or of very sensitive and accurate areas such as tip area, the CFD method plays an essential role as evidenced in the research. Figure 11(a)–(c) depends only on the papers that are used in this work. A detailed summary of CFD studies of W-T is given in Table VIII.

5.5. Validation of CFD models

The most validation cases are cited for self-rectifying W-T that are performed at Saga University in Japan [74,201]. The experimental work is performed at a test rig capable of producing reversing air flows. The flow is produced by the reciprocating motion of a piston in a large cylinder

(1.4 m diameter, 1.7 m long) [71,202]. The piston can be driven back and forth by means of three ball screws acted upon by a DC servomotor. A computer controls the motor to produce any air flow velocity. A settling chamber is located between the cylinder, and the 300-mm diameter turbine test section. Many of CFD investigations employ this experimental work as a validation case such as T. H. Kim, et al. [76,113] and Zahari Taha, et al. [139,140], in addition to several other CFD works in [77,81,82,129,134,135].

Other experimental works that are also often used as validation cases can be found in [97]. A larger rig was constructed in 1992 at Instituto Superior Técnico, Lisbon, where W-T (rotor diameter 0.6 m) was tested in a unidirectional flow. The turbine pressure drops, and air flow rates are supplied by a centrifugal fan fitted with a variable-speed controller. The turbines were mounted in an open-ended annular duct that led to a plenum chamber. The chamber contained a honeycomb lattice that straightened the air flow entering the calibrated nozzle (both designed according to AMCA 210/67 standard), which was situated upstream of the exhaust outlet. The 0.67-m long nozzle contracted from 0.8 to 0.4 m while the plenum chamber was 2-m long, 1.72-m high, and 1.78-m wide. The turbines were connected via a torque meter to a motor-generator whose speed could be varied continuously. The double-shaft turbines were fitted with an extra bearing assembly, torque and speed transducer, and a generator for the upstream rotor. These experimental work data can be found in many validation cases such as Paresch Halder, et al. [203–205] and S. Shaaban [99,146], and M. Torresi, et al. [37,91].

Table VIII. Detailed summary of CFD studies of W.T.

Reference/Year	Turbulence model	Reynolds number	Number of Elements	Blade profile	Boundary condition
[100]/1996	K-Epsilon model together with a modified low Reynolds number model	$8 \cdot 10^5$	449,736	NACA0015	3D-unsteady
[110]/1997	K-Epsilon model together with a modified low Reynolds number model	$8 \cdot 10^5$	436,000	NACA0015	3D-unsteady
[130]/2001	RNG K-Epsilon model	$5 \cdot 10^5$	80,000	CA9	3D-steady
[75]/2002	K-Epsilon model	NA	400,000	NACA0012, NACA0015, NACA0021	3D-unsteady-(time step = 0.001 s-sinusoidal wave)
[113]/2002	K-Epsilon model with a modification model	Low Reynolds number	70,000 nodes	NACA0020, CA9	3D-steady
[76]/2002	RNG-SGS model	$2.4 \cdot 10^5$	560,000	NACA0015, NACA0020	3D-unsteady-($f = 0.167$ – one-half period of the sinusoidal wave)
[80]/2003	RNG-SGS	$2.4 \cdot 10^5$	560,000	NACA0020	3D-Unsteady-($f = 0.167$ – one-half period of the sinusoidal wave)
[77]/2003	RNG-SGS model	$2.4 \cdot 10^5$	560,000	NACA0020, NACA0015	3D-Unsteady ($f = 0.167$ – sinusoidal wave)
[81]/2004	LES-RNG-SGS model	$2.4 \cdot 10^5$	560,000 (monoplane)–720,000 (biplane)	NACA0020	3D-Unsteady-($f = 0.167$ – half period of the sinusoidal wave)
[82]/2004	LES and RNG-SGS model	$2.4 \cdot 10^5$	560,000 (monoplane) –720,000 (biplane)	NACA0020	3D-Unsteady-(one-half period of the sinusoidal-)
[91]/2004	K-Omega SST	539,233	163840	NACA0015	3D-steady (two sinusoidal wave-0.8 and 1.2 m wave height-2.275 and 3.413 m/s ;axial velocity)
[101]/2005	K-Epsilon model	NA	620,000	NACA 0021	3D-steady
[128]/2006	K-Epsilon model.	From $1.0 \cdot 10^5$ to $3.8 \cdot 10^5$	560,000 and 580,000	NACA0020 with end plate	3D-steady
[129]/2007	RNG-K-Epsilon model	$2.5 \cdot 10^5$	570,000	NACA0020 with end plate	3D-steady
[98]/2008	SST model	$2.4 \cdot 10^5$	25600	(AOP) based on NACA 2421	2D-steady
[37]/2008	Spalart Allmaras	NA	1,092,352	NACA0015	3D-steady
[36]/2009	Spalart Allmaras, K-Omega SST	$2 \cdot 10^5$	$2 \cdot 10^6$, $2.4 \cdot 10^6$, and $4.1 \cdot 10^6$	NACA0015	3D-steady
[139]/2010	Realizable K-Epsilon	From $0.74 \cdot 10^5$ to $4.41 \cdot 10^5$	295,500	NACA0020	3D-steady
[38]/2011	k-SST model	From 34833 to 42199	$4 \cdot 10^6$	NACA0015	3D-steady
[134]/2011	Realizable K-Epsilon	$2.4 \cdot 10^5$	Between 60,000 and 80,000	NACA 0021 (AOP)	2D-steady

(Continues)

Table VIII. (Continued)

Reference/Year	Turbulence model	Reynolds number	Number of Elements	Blade profile	Boundary condition
[140]/2011	Realizable <i>K-Epsilon</i>	From $0.68 \cdot 10^5$ to $4.41 \cdot 10^5$	295,500.	NACA0020	3D-steady
[105]/2012	Realizable <i>K-Epsilon</i>	NA	424,686	NACA 0021	3D-steady
[231]/2012	SST transitional model	120,000	$3.5 \cdot 10^6$ (nodes)	NACA 0021	3D-unsteady (time-step = $5 \cdot 10^{-5}$)
[99]/2012	Realizable <i>K-Epsilon</i> model and the Reynolds stress	NA	1,236,576	NACA0015	3D-steady
[146]/2012	Realizable <i>K-Epsilon</i> model	NA	1,131,540	NACA0015	3D-steady
[141]/2013	K-Omega SST	From $1.4 \cdot 10^5$ to $2.8 \cdot 10^5$	NA	NACA0020	3D-steady
[126]/2013	Realizable <i>K-Epsilon</i> turbulence model	$2.4 \cdot 10^5$	60000–80000	NACA0021 (AOP)	2D-steady
[127]/2013	Realizable <i>K-Epsilon</i> turbulence model	$2 \cdot 10^4$	2D – 60,000 and 80,000	NACA0021 (AOP)	3D–2D-steady
[114]/2013	Standard fully turbulent shear-stress transport turbulence model	$5.0 \cdot 10^5$	3D – 1,348,760 and 1,404,690 for (AOP)	Hub: NACA0018-63 Midspan: NACA0015-63	3D-steady
[232]/2013	SST-turbulence model	$5.4 \cdot 10^5$	1.8 million	Tip: NACA0012-63 Hub: NACA0021-63 Mid: NACA0018-63 Tip: NACA0015-63	3D-steady
[109]/2014	Realizable <i>K-Epsilon</i> model	From $6 \cdot 10^4$ to 410^5	312,951	NACA0012, NACA0015, NACA0020 and NACA0021	2D-steady
[135]/2015	RNG- <i>K-Epsilon</i> model	NA	238,876 and 207,638	NACA0020 and variable chord airfoil	3D-steady
[203]/2015	K-Omega SST	NA	1,424,016	NACA0015	3D-steady
[204]/2015	K-Omega SST	NA	NA	Modified blade	3D-steady
[211]/2015	Transition SST model	From $0.8 \cdot 10^5$ to $1.5 \cdot 10^5$	NA	NACA 0015	3D-unsteady-T = 9 s
[205]/2015	K-Omega SST	1,368,000	1,424,016	NACA0015	3D-steady
[108]/2016	Realizable <i>K-Epsilon</i> model	From $6 \cdot 10^4$ to $4 \cdot 10^5$	312,951	NACA0012, NACA0015, NACA0020 and NACA0021	2D-unsteady-T = 6.7 s

The breakwater built in the natural laboratory of Reggio Calabria (at Politecnico di Bari University – DIMEG Department) was 16.3-m long, and it is realized by nine caissons close to each other [93]. Each caisson consists of three interconnected cells, where air can flow from one cell to another of the same caisson through holes. The central caisson is equipped with a small scale prototype of W-T, placed in a duct connected to the central cell of the caisson. The turbine hub is made up of aluminum and is obtained from a commercial fan. The blades have been produced with composite material reinforced by carbon fiber with suited attachment [206,207]. In addition to the experimental work, M. Torresi and S.M. Camporeale implemented the CFD method to examine the performance of W-T in [36,38].

The experimental setup consists of a 4-kW variable speed centrifugal blower for delivering the necessary pneumatic power to the W-T [101,208,209]. The blower is capable of developing an optimum static pressure rise of about 2000 N/m^2 while delivering a discharge of $1.1 \text{ m}^3/\text{s}$. The delivery duct of the centrifugal blower is 2800-mm long and has a diameter of 250 mm. A diverging cone of length 25 mm connects this duct with the turbine test section. The validation result can be found in Z. Carija, *et al.* [105] and T. S. Dhanasekaran, *et al.* [101].

The experimental setup was carried out on a turbine enclosed in a cylindrical annular duct, with an axial flow fan mounted at the exit of the duct [164]. The turbine was mechanically connected to an electric generator/motor by a belt drive. Turbine rotors were tested with 4, 6, and 8 blades of constant chord. The blades were made of fiberglass with a good surface finish. TC was about 1 mm. The rotor hub was a disk whose axial length at the periphery was 50 mm. In the four-bladed and six-bladed configurations, the turbine was found to be unable to reach full rotational speed on its own as a consequence of its net torque being negative or too

small at intermediate speeds. The electrical machine was then used as a motor for starting purposes. J. K. Watterson, *et al.* used these experimental data to validate their CFD work in [110].

The most recent experimental setup was performed by the Department of Mechanical, Chemical and Materials Engineering of the University of Cagliari. This work can simulate the real operation of a wave energy conversion device based on the principle of an (OWC) equipped with a W-T [107,210]. Wave motion is reproduced by means of a piston moving inside a chamber generating the periodic bidirectional airflow through the turbine. The turbine drives a three-phase induction machine controlled by an inverter with encoder feedback. The wave Characteristics – defined by the shape, amplitude, and frequency of the piston motion – can be modified by adjusting the parameters of the hydraulic control unit to obtain a maximum flow velocity in the range of 10–20 m/s. The setup is instrumented with different sensors allowing measurement of torque, angular velocity, piston position, and static pressure, total pressure and flow direction upstream and downstream of the rotor with aerodynamic probes. The flow field characteristics are measured by introducing aerodynamic probes in the sections located upstream and downstream of the turbine at a distance of about 20 mm from the impeller. This experimental work is also used as a validation case by T. Ghisu, *et al.* in [211]. Table IX demonstrates the geometric details for six experimental works that were often used for the CFD validation cases.

6. DISCUSSION

Over 230 studies are investigated in this work. By collecting data about its main methodology, we can

Table IX. Geometric details for CFD validation cases.

Validation Case	Blade profile	C (mm)	R_h (mm)	Z	σ	R_t (mm)	Reynolds number	Note
[71,74,201,202]	NACA0020	90	104.5	6	0.67	149	$2.4 \cdot 10^5$	Aspect ratio = 0.5
[97]	NACA 0015	125	200	8	0.64	294	$6.5 \cdot 10^5$ and $3.9 \cdot 10^5$	Tip clearance of 1 mm Angular velocity = 2000 rpm
[93,206,207]	NACA 0015	74	101	7	0.64	155	$2 \cdot 10^5$	Tip clearance = 2% from chord length
[101,208,209]	NACA 0021	100	81.5	4	0.6	131.5	NA	Tip clearance of 1 mm Angular velocity = 4500 rpm
[164]	NACA 0012	100	150	4, 6, and 8	0.29, 0.44 and 0.59	296.5	$5.6 \cdot 10^5$	Rotational speed = 2700 rpm Tip mach number 0.25
[107,210]	NACA 0015	36	95	14	0.729	125	Between $0.8 \cdot 10^5$ and $1.5 \cdot 10^5$	Piston period between 7 and 9 s

classify the role of CFD in each research parameter. Guide vanes before and after the rotor may be one of the most effective devices to improve turbine performance. However, literature records do not show any CFD studies of guide vanes. For the hysteretic behavior, it can be concluded that several parameters have effects on the performance of W-T in bidirectional airflow, but the most important one appears to be the hysteresis effect. Figure 12(1) shows the use of CFD compared with experimental measurement in studying hysteretic behavior.

The multiplane W-T is required to improve the performance, and especially the contra-rotating one. The CFD method appears in recent research (for this section) to yield more accurate results. In addition, we can improve the performance of W-T by investigating the flow field through the turbine and its parts by studying the flow characteristics at different operating conditions, such as Reynolds number, Mach number, flow coefficient, and angle of attack and flow direction, and also by studying the stall condition, the starting behavior and the Tip leakage flow effect. More than 65% of the aforementioned studies depend on the CFD method to predict the behavior of the flow through the turbine, even in the 1990s, see Figure 12(2).

The design optimization section includes four parts; it can be concluded from this part that the most important parameters effect on the performance of W-T is the turbine blade solidity. Blade thicknesses, hub to tip ratio and the size of turbine also have effects on the performance of W-T. The change in previous parameters to improve the performance is the basic step to design optimization, so most of this research is conducted in 1980s and 1990s, and therefore, the CFD method has a very modest effect. The position of blade, according to the hub centerline, has a direct effect on the performance of turbines, and it is shown in the second part of position-based parameters. Setting the blades at their optimum pitch angle during compression and suction is expected to substantially

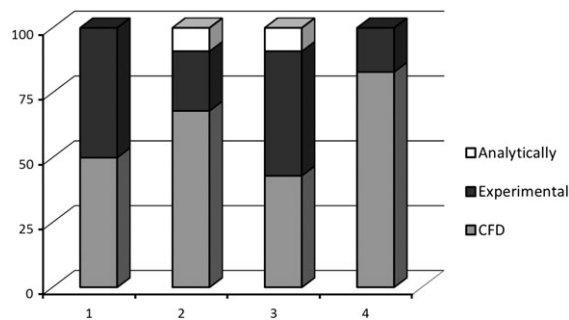


Figure 12. (1) Classification of research: 15 papers discussing the hysteretic behavior according to the main methodology of each paper. (2) Classification of research: 13 papers discussing the flow through turbine according to the main methodology of each paper. (3) Classification of research: 24 papers discussing the design optimization according to the main methodology of each paper. (4) Classification of research: seven papers discussing the tip clearance according to the main methodology of each paper.

improve W-Ts' efficiency. It is clear that there is a tendency to the CFD method in recent research in addition to taking an important role in the formation of the optimization code. Moreover, the peak efficiency of W-T increases by attaching end plate to its blade.

Finally, the non-symmetric airfoils, in an attempt by the researchers to improve the overall performance of turbine, non-traditional airfoil, are investigated. CA9, HSIM 15-262123-1576, and other optimum airfoil have been used to achieve this purpose. As a conclusion for design optimization with its four parts, the CFD method has been used in all parts from the 1990s till now to complete the experimental work in an easier and a cheaper way, see Figure 12(3). In addition, it gives very promising results in terms of increasing the overall turbine performance, especially the optimum shape part. Therefore, there is a need to conduct more investigation and to use other different methods for optimization. In other words, design optimization is the key for future study.

The studies underline the importance of the optimization of the TC in order to improve the turbine performance in terms of torque coefficient and efficiency, because of the sensitivity of W-T to TC. The effect of TC on the W-T system was ascertained long time ago, but no method is like the CFD to investigate this phenomenon; therefore, more than 80% of the studies use the CFD method. In addition, the increased possibilities and the development of CFD method increase the study and understanding of this phenomenon, see Figure 12(4).

When W-T is compared with the impulse turbine, the latter has a higher overall performance. But this point will be discussed in details in the next part. The experimental and numerical simulation analysis is used to investigate in this issue.

In view of the previous research in the section of the connections with other turbines, it can be concluded that the efficiency of W-T is higher than that of the impulse turbine when the flow coefficient is less than the stall point. But after the stall point of W-T, the efficiency of the impulse turbine is considerably higher than that of W-T. In other words, W-T can extract power at a low air flow rate, when other turbines would be inefficient, as shown in Figure 13. In addition, it is relatively cheap to construct.

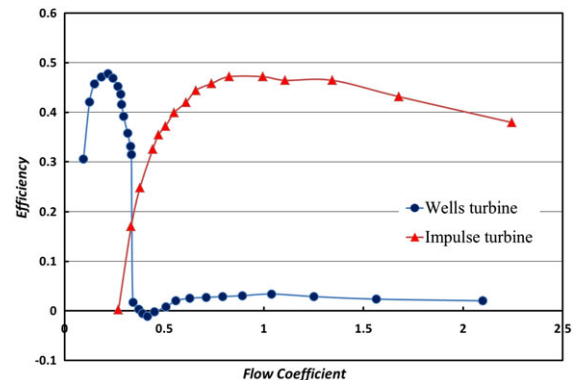


Figure 13. Turbines characteristics under steady flow conditions: flow coefficient variation with the efficiency [26].

7. CONCLUSION

A comprehensive review for the W-T is presented in this paper. The literature references are categorized according to the research approaches to different W-T components, and according to the research methods investigating W-T. Because CFD is a widely used approach in W-T research, an independent section of the review is devoted to comparatively discuss the methods and techniques. The following remarks can be concluded from the review:

- W-T components play vital roles in performance and efficiency. Each component requires a rigorous optimization practice to harvest possible additional efficiency enhancement.
- Guide vanes and multistage of W-T that have the same direction of rotation are used to increase the efficiency; in addition, the two-stage W-T has an opposite direction.
- The increase in Reynolds number, Mach number, flow coefficient, and angle of attack leads to an increase in the efficiency of W-T, until a certain critical value.
- Determining the optimum position of end plate and the optimum value of blade sweep ratio, TC, blade skew and setting pitch angle increases the efficiency of W-T. However, the numerical optimization process is used to create optimum non-symmetric airfoil.
- The use of W-T in low-flow coefficient period and impulse turbine in high-flow coefficient period increases the overall performance of OWC system.
- The global entropy generation rate due to viscous dissipation is a very sensitive indicator for W-T behavior at any change in design parameters, the operating condition and also being affected by flow direction.

NOMENCLATURE

A	= the total blade area = (z c b), m ²
A _r	= rotor area = πR_m^2 , m ²
A	= margin distance for the end plate, m
b	= blade span, m
c	= blade chord, m
C _D	= drag force coefficient = $\frac{D}{\frac{1}{2}\rho(V_r)^2 A}$
C _L	= lift force coefficient = $\frac{L}{\frac{1}{2}\rho(V_r)^2 A}$
C _P	= power coefficient
C _T	= torque coefficient
D	= drag force, N
D _r	= rotor diameter, m
f	= wave frequency, Hz
F _A	= axial force = $\frac{1}{2}\rho V_r^2 A C_A$, N
F _t	= tangential force = $\frac{1}{2}\rho V_r^2 A C_t$, N
g	= leading edge offsetting of a blade from an axis, m
I	= moment of inertia, kg m ²
K	= non-dimensional period

L	= lift force, N
Δp	= pressure difference across the turbine = $\frac{F_A}{Area}$, N/m ²
Q	= flow rate through the rotor area, m ³ /s
R _h	= rotor radius at hub, m
R _m	= mean rotor radius = $\frac{R_t + R_h}{2}$, m
R _r	= rotor radius, m
R _t	= rotor radius at tip, m
T	= time period = $1/f$, sec
t	= rotor blade thickness, m
T _L	= loading torque N m
TSR	= tip speed ratio = $\frac{\omega R_m}{V_{Am}}$
V _A	= axial velocity = $V_{Am} \sin(\frac{2\pi t}{T})$, m/s
V _{Am}	= maximum value of axial velocity, m/s
V _r	= Resultant air velocity = $\sqrt{V_A^2(t) + \omega^2(t)R_m^2}$, m/s
W*	= output power coefficient
X _i	= inertia coefficient
X _L	= loading torque coefficient = $\frac{T_L}{\rho\pi R_m^3 V_{Am}^2}$
Z	= number of blades
α	= angle of attack- the angle between the chord line and the direction of the fluid velocity, degree
η	= mean turbine efficiency
ρ	= air specific density, kg/m ³
σ	= turbine solidity = $\frac{Z C}{2\pi R_m}$
φ	= flow coefficient = $\frac{V_{Am}}{\omega_{avr} R_m}$
ω	= rotor angular speed, rad/s
$\frac{\omega}{\omega^*}$	= non-dimensional angular velocity under irregular flow condition

List of Abbreviations

AOP	= an optimized profile
AR	= aspect ratio (the ratio of span to chord)
CFD	= computational fluid dynamics
NACA	= National Advisory Committee for Aeronautics
OWC	= oscillating water column
TC	= tip clearance
W-T	= Wells turbine

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